Modelling heat and salinity related convective processes in deep mining flooded wells

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Abstract The twenty-first century sees a generalization of the consideration of sustainable development issues. In the Lorraine Coal Basin (France) after an intensive mining activity, the cessation of mine water extraction has led to the flooding of old mining exploitations: the resulting reservoirs could be valorized by using a geothermal solution. In this context, characterizing and modelling the thermal-hydrodynamic-chemical functioning of those reservoirs are primordial. Convective processes in the Vouters 2 well account for its temperature and electric conductivity logs. Logs profiles are interpreted as a thermohaline staircase, which can appear when salinity and temperature gradients both increase with depth.

Key Words flooded mine, modelling, convection, heat, hydrodynamics, Lorraine

Introduction

In Lorraine (France), industrial mining began in the 19th century and reached a peak in the 1960s, followed by a decline that had finally led to mines closure in the 1980s-1990s. Today, two main facts can lead to a geothermal solution: (i) flooded coal mines represent a major water resource and (ii) the search for non-fossil new energies coincides with the end of the coal extraction cycle in this region.

Many approaches for modelling the functioning of flooded reservoirs exist. An investigation uses physically-based distributed flow and solute-transport models, considering that flow and transport take place only in channel or pipe networks (Hamm et al. 2008). More complex developments consider interactions between the porous media and the flooded mine workings through coupling continuum porous media with a box model (Brouyère et al. 2009) or a pipe-network model (Adams et al. 2001) used for mine conducts. Before considering a larger scale where the well interacts with the surrounding mine network and porous medium, our study is currently focused on the functioning of a well with its connected entrances and associated inflows or outflows of water. Complex convective processes can occur in wells (Wolkersdorfer 2008) and common modelling approaches are not suitable. The software used for simulating flow, heat and transport in the well is COMSOL Multiphysics®, which is able to deal with many different coupled physics.

Site description

The Lorraine coal basin is located along the eastern edge of the Paris Basin (France). It covers an area that is 140 km long (W-E) and 70—80 km wide. The Lorraine coal-bearing deposit dates from the Westphalian and Stephanian (Carboniferous) and is formed of intercalated veins in a complex sequence of argillites, sandstones and conglomerates of laterally various nature and thickness. The north-east fraction of the deposit was the only part exploited as it is shallower (80 m deep minimum) than western deposits (up to 1400 m deep) which are increasingly buried under upper Permian conglomerates overlain by the Trias sandstone and limestone aquifer formation. Due to fracturation and partial destruction of the Permian conglomerates, collapsed zones enabled water from the Trias sandstone aquifer to infiltrate into the mine galleries. A major folding phase called Saalian phase occurred at the end of the Hercynian compression and accounts for the numerous faults of the basin, the most important ones delimiting the exploitation areas, as the WNW Saint Nicolas fault and the NE-SW Hombourg fault in the studied zone of the Vouters 2 and Simon 5 reservoirs (respectively SW and NE rectangles in fig.1). 58 wells were bored in the concession, 3 of them still accessible and useful for the study: Vouters 2, Marienau and Simon 5 (respectively labeled V, M and S in fig. 1).

As for water chemistry in the site, samples taken in the mine during its exploitation highlight three main types of water (Fabriol 2008): (i) low mineralized water coming from the Trias sandstone aquifer, (ii) sulfate-rich water resulting from flows in the mine and (iii) highly mineralized water found in the lowest levels of the mine.

Double-diffusive convection (DDC)

Briefly, there are broadly two regimes for DDC (Love et al. 2007): monotonic convection (sometimes referred to as the fingering regime) and oscillatory convection.
DDC can occur where the density of the fluid is affected by at least two components with different diffusivities. Combined heat and salt transport (thermohaline convection) is one specific subset of the more general DDC problems. In thermohaline phenomena, the thermal diffusivity $D_T$ (m²/s) is approximately two orders of magnitude higher than the solute diffusivity $D_S$ (m²/s). Under certain conditions, this may result in gravitational instabilities due to the phase lag between the faster diffusing heat and the slower diffusing solute.

If one considers a parcel of hot salty water that is displaced upward, the parcel will diffuse heat more rapidly than it diffuses salt, which will result in instability across the interface. As the perturbed parcel of water still rises (losing heat more rapidly than it loses salt) it eventually becomes heavier than the surrounding fluid at which point it begins to descend. The parcel of water will descend beyond its original position, warming as it sinks. The parcel eventually becomes less dense than the surrounding fluid at which point it begins to rise again. An oscillatory motion results.

The initial instability starts as a growing oscillation near the bottom (Kundu 1990). As the heating is continued beyond the initial appearance of the instability, a well-mixed layer develops (as shown for Vouters 2 in A – fig. 2), capped by a salinity step and a temperature step. The heat flux through this step forms a thermal boundary layer (A – fig. 2). As the well-mixed layer grows, the temperature step across the thermal boundary layer becomes larger. Eventually, the Rayleigh number across the thermal boundary layer becomes critical, and a second convective layer forms on top of the first (B – fig. 2). The second layer is maintained by heat flux (and negligible salt flux) across a sharp laminar interface on top of the first layer. This process continues until a stack of horizontal layers forms one upon another. From comparison with the Bénard convection, it is clear that inclusion of a stable salinity gradient has prevented a complete overturning from top to bottom. In the case of the Vouters 2 well, the location of the sharp interfaces corresponds to gallery entrances (C – fig. 2), suggesting that convection is forced by incoming water flows at those levels.

**Conceptual model of the mine shaft**
The well is modelled as a vertical circular cylinder (fig. 3) whose top and bottom are rigid and at constant temperature and constant concentration and whose lateral wall is impermeable and rigid and at a constant temperature and constant con-
A basic solution \((\phi_0, P_0, T_0, S_0, \rho_0)\) is obtained: constant temperature, hydrostatic pressure, and salinity and density fields without any motion of the fluid. This solution is perturbed by a small amount \((\phi', P', T', S', \rho')\) to become \((\phi, P, T, S, \rho)\). Small disturbances from the basic solution satisfy the set of equations

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\[
\begin{align*}
\vec{\rho}, \vec{\rho} &= 0 \\
\frac{\partial \vec{v}}{\partial t} + (\vec{v} \cdot \nabla) \vec{v} &= -\frac{\vec{\rho} p}{\rho_0} + \rho \vec{g} + \nu \vec{\nabla}^2 \vec{v} \\
\frac{\partial T}{\partial t} + (\vec{v} \cdot \nabla) T &= D_T \nabla^2 T \\
\frac{\partial S}{\partial t} + (\vec{v} \cdot \nabla) S &= D_S \nabla^2 S.
\end{align*}
\]

where \(\Delta T\) and \(\Delta S\) are the temperature and salinity gaps between top and bottom of the water column, \(Pr = \upsilon / DT\) is the fluid Prandtl number and \(Le = D_s / DT\) the Lewis number. The thermal and solutal Rayleigh numbers \((Ra_T\) and \(Ra_S)\) are defined by

\[
Ra_T = \frac{g \beta H_2^2 \Delta T}{\nu D_T}, \quad Ra_S = \frac{g \beta H_2^2 \Delta S}{\nu D_S}.
\]

Stability criteria (Love et al. 2007) mostly based critical, thermal and solutal Rayleigh numbers are used to choose adapted aspect ratio (radius \(r\) of the well divided by the length \(H_f\) of the water column) and to weigh respective influences of temperature and salinity gradients (represented by \(\Delta T\) and \(\Delta S\)). Parameters values of Vouters 2 were tested with these criteria and maintain the occurrence of oscillatory double-diffusion. The well has a 3.75 m radius for a 900 m high water column. The temperature gradient is the local geothermal one of 3 °C/100 m and the salinity gradient is taken at 0.119 mol/m⁴ (or 11 mg/L/m), based on averaged values for different wells in the basin.

Simulation results
In order to study different convective processes, we activated separately the temperature gradient

\[
\rho = \rho_0 (1 - \alpha (T - T_0) + \beta (S - S_0)),
\]

where \(\rho, \rho_0, \alpha, T, T_0, \beta, S, S_0\) are respectively the density \((\text{kg/m}^3)\), reference density, thermal expansion coefficient \((\text{K}^{-1})\), temperature \((\text{K})\), reference temperature, solute expansion coefficient \((\text{m}^3/\text{mol})\) and reference salinity.

Velocity \(\vec{v}\), pressure \(P\), temperature \(T\) and salinity \(S\) depend on the set of equations.
and the salinity gradient before combining them. Water entrances in the well were added to test appearance of steps at these levels. Free thermal and free solutal convection simulations give good results, with development of convection cells in the water column (A - fig. 4). Velocities are observed and have a mm/s magnitude. Thermosolutal convection simulation results do not show thermohaline staircase at the date of the article, even if convection cells similar to those of free thermal convection can be observed. The presence of an additional gallery entrance does not trigger the phenomenon, but can make forced convection overpower free convection if inflow velocity is too high, with a cm/s magnitude here (B - fig. 4).

Conclusions
The Lorraine coal-basin is a complex hydrogeological system, formed by the superposition of a sandstone aquifer formation flowing through fractured conglomerates down to the flooded mine. We have selected a quasi-isolated reservoir from the entire exploited area to model its thermal-hydrodynamic-chemical (THC) functioning. Interpretation of electric conductivity-temperature logs in the Vouters 2 well highlighted the presence of free double-diffusive oscillating convection due to coupled actions of salinity and temperature gradients. A numerical model is being built to understand this phenomenon and its impact over the whole Vouters 2 reservoir. Thermal convection or solutal convection is properly reproduced in a water column with or without forced flows, though the combination of both convections does not produce a thermohaline staircase yet. Current efforts are focused on setting adapted parameters for the COMSOL solver. We are also building up a digital three-dimensional geometry model and intend to integrate the simulation results into the future THC model.

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![Figure 3 Conceptual model of a 2D vertical cylindrical well and associated boundary conditions.](image)

**Figure 3** Conceptual model of a 2D vertical cylindrical well and associated boundary conditions.

![Figure 4 Free thermal convection (A) and mixed thermosolutal convection (B): streamlines showing convection cells.](image)

**Figure 4** Free thermal convection (A) and mixed thermosolutal convection (B): streamlines showing convection cells.
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References